A Theoretical Model for the Increases in Cutting Edge Recessions During Milling of Nine Species of Wood

Bolesław Porankiewicz, a,b Daria Wieczorek, a Anita Bocho-Janiszewska, c Emilia Klimaszewska, c Chiaki Tanaka, d and Wayan Darmawan e

The high-speed steel (HSS) cutting tool edge recession increase ($\Delta VB$) from milling wood of nine wood species with very different properties were analyzed. Theoretical simulations showed that the synergistic effect of the wood density ($D$), hard mineral contamination (HMC), and high temperature tribochemical reactions (HTTR), as well as initial edge recessions were important factors that accelerated wearing on the examined cutting edges.

Keywords: Cutting edge recession; High speed steel; Wood; Milling; High temperature tribochemical reactions

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INTRODUCTION

Wood cutting tool edge wearing and the role of the high temperature tribochemical reactions (HTTR) and hard mineral contaminations (HMC) during wearing has not been fully explained nor quantified. Cristóvão et al. (2009) and Cristóvão et al. (2011) are good examples of recent works in which the dulling of fast cutting tools after machining wood specimens from tropical forests was associated mainly with large HMC, but the influence of the HTTR and the size of the HMC particles were not taken into account, despite several publications on this subject (Porankiewicz et al. 2005, 2006, 2008). The fast wearing of cutting tools in the cited works was attributed not only to the HMC, the HHTTR, and the size of the HMC particles, but also to the synergistic effect of chemical and mechanical factors on wear. Another reason for this problem, which has not been solved yet, is the limited amount of wood specimens examined. Recent repetitions of the thermal gravimetry analysis (TGA) for several solid wood species originating from Indonesia and Japan, together with carbonyl iron powder, show major differences in comparison to results of tests reported in previous works (Porankiewicz et al. 2005, 2006, 2008), so there is a presumption that this diversity may not be related to properties of examined wood specimens. In the present work the mechanism of the HSS tool cutting edge recessions after longitudinal milling, reported in previous experiments (Porankiewicz et al. 2005, 2006, 2008), were reanalyzed. Of the HMC, the HTTR and the density ($D$), and some mechanical properties of wood specimens that were examined, some were very small and some very great.
EXPERIMENTAL

Machine tests were performed by Dr. Jakub Sandak and Dr. Piotr Iskra in the laboratory of Shimane University, Matsue, Japan, using a Shoda Fanuc NC-3 computer numerical controlled machine (Hamamatsu, Shizuoka, Japan; Fig. 1) under the following machining conditions: rotation speed of a spindle \((n)\), 2,864 \(\text{min}^{-1}\); cutting speed \(\left(v_C\right)\), 30 \(\text{m/s}\); number of cutting edges \((z)\), 1; feed rate per tooth \((f_z)\), 0.1 mm; rake angle \((\gamma_F)\), 30°; sharpness angle \((\beta_F)\), 55°; cutting depth \((g_S)\), 1.5 mm; and moisture content \((m_C)\), 11%. The materials of the cutting edge SKH51 were according to JIS G64403. The hardness of the cutting edge material was 64 HRC.

![Fig. 1. Cutting machine diagram. 1) cutting tool, 2) working piece, 3) machine table, and 4) electrical motor](image1)

The main properties of wood specimens of nine wood specimens are shown in Tables 1 and 2. Images of sections perpendicular to grains are shown in Fig. 2.

![Fig. 2. Scan of sections perpendicular to grains of wood specimens examined: 1 - Ebony; 2 - Hornbeam; 3 - Keirung; 4 - Tamo; 5 - Yellow Meranti; 6 - Japanese Douglas Fir; 7 - Kempas; 8 - Keyaki; 9 – Oilpalm](image2)

**Table 1. Wood Specimens Examined**

<table>
<thead>
<tr>
<th>no.</th>
<th>Name</th>
<th>Name</th>
<th>Country of origin</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Ebony</td>
<td>Diospyros celebica</td>
<td>Indonesia</td>
</tr>
<tr>
<td>2</td>
<td>Hornbeam; Shide</td>
<td>Carpinus sp.</td>
<td>Japan</td>
</tr>
<tr>
<td>3</td>
<td>Keirung</td>
<td>Combretocarpus sp.</td>
<td>Indonesia</td>
</tr>
<tr>
<td>4</td>
<td>Tamo</td>
<td>Sassafras albidum</td>
<td>Japan</td>
</tr>
<tr>
<td>5</td>
<td>Yellow Meranti</td>
<td>Shorea faguetiana</td>
<td>Indonesia</td>
</tr>
<tr>
<td>6</td>
<td>Japanese Douglas Fir; Kuromatsu</td>
<td>Pseudotsuga douglasii</td>
<td>Japan</td>
</tr>
<tr>
<td>7</td>
<td>Kempas</td>
<td>Koompasia malaccensis</td>
<td>Indonesia</td>
</tr>
<tr>
<td>8</td>
<td>Keyaki</td>
<td>Zeikova serrata</td>
<td>Japan</td>
</tr>
<tr>
<td>9</td>
<td>Oilpalm</td>
<td>Elaeis guineensis</td>
<td>Indonesia</td>
</tr>
</tbody>
</table>
For the estimation of the HTTR of products of thermal degradation of wood towards iron, a method based on the TGA was used, as described in earlier works (Porankiewicz 2003a; 2003b). The HTTR peaks were recognized as a rapid mass ($m$) increased on a first derivative (d$m$/dt) of the $m$ against time, $t$ (min) plots (dTG). Figure 3 shows peaks of the HTTR. For the characterization of the HTTR of products of thermal decomposition of wood and iron, a binder of the cutting edge material, the following quantifiers were examined: $R_{MX}$ - maximum; $R_{MI}$ - minimum; $R_{Xs}$ - average of three maximums; $R_{Ws}$ - average of weights according to temperature of maximum, $T_X$; $R_{As}$ - average of maximum corrosion peaks area; $R_{Ss}$ - average of all corrosion peaks. These quantifiers were calculated according to Eqs. 1 through 6,

$$R_{MX} = r_{xj} \cdot m^{-1} \text{ (min}^{-1} \text{)}$$  \hspace{1cm} (1)

$$R_{MI} = r_{ij} \cdot m^{-1} \text{ (min}^{-1} \text{)}$$  \hspace{1cm} (2)

$$R_{Xs} = \Sigma(r_{xj} \cdot m^{-1}) \cdot 3^{-1} \text{ (min}^{-1} \text{)}$$  \hspace{1cm} (3)

$$R_{Ws} = \Sigma[(r_{xj} \cdot T_{xj}) \cdot m^{-1}] \cdot (3 \cdot \Sigma T_{xj})^{-1} \text{ (min}^{-1} \text{)}$$  \hspace{1cm} (4)

$$R_{As} = \Sigma A_{ij} \cdot 3^{-1} \text{ (mg} \cdot \text{1}^0 \cdot \text{min}^{-1})$$  \hspace{1cm} (5)

$$R_{Ss} = \Sigma[\Sigma (r_{xj} \cdot m^{-1}) \cdot n_{ij}^{-1}] \cdot 3^{-1} \text{ (min}^{-1} \text{)}$$  \hspace{1cm} (6)

where $m$ is the mass of iron powder specimen (mg); $r_{xj}$ and $T_{xj}$ are, respectively, the maximum height and temperature of corrosion peak after maximum mass degradation (point $M$ in Fig. 3) in repetition $j$ (mg/min); $r_{ij}$ is the maximum height corrosion peak indexed by $i$ (including peaks before and after point $M$ in Fig. 3) in the repetition $j$ (mg/min); $A_{ij}$ is the area of corrosion peak indexed as $i$ (including peaks before and after point $M$) in the repetition $j$ (Fig. 3); $j$ is the index for the repetition; $n_{ij}$ is the number of corrosion peaks taken into account in one repetition $j$. The number of TGA repetitions performed was $j = 3$.

The $R_{Xs}$, the $R_{MX}$, the $R_{MI}$, and the $R_{Ss}$ quantifiers, according to Eqs. 1 through 3 and 6, appear as the relative speed of the $Fe$ specimen mass increase in the corrosion peaks. For the evaluation of the $R_{Xs}$, the $R_{MX}$, the $R_{MI}$, $R_{Ws}$, and $R_{As}$ quantifiers, corrosion peaks in the temperature range of 276 °C to 309 °C were taken into account. For quantifier $R_{Ss}$

<table>
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<tr>
<th>no.</th>
<th>$D$ (kg·m$^{-3}$)</th>
<th>$MOR$ (MPa)</th>
<th>$E$ (GPa)</th>
<th>$CS$ (MPa)</th>
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<td>14.17</td>
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<td>520</td>
<td>74.6</td>
<td>8.24</td>
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<td>11.30</td>
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<td>11.76</td>
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<td>9</td>
<td>395</td>
<td>36.1</td>
<td>4.59</td>
<td>4.3</td>
</tr>
</tbody>
</table>

$D$ - (kg·m$^{-3}$), $MOR$ - Modulus of Rupture by Bending (MPa), $E$ - Modulus of Elasticity (GPa), $CS$ - Compression Strength (MPa)
corrosion peaks were also taken into account, before and after point $M$ in Fig. 3, which were from 202 °C to 223 °C and from 395 °C to 416 °C, without small peaks (narrow and short), marked in Fig. 3 as 'S'.

![Fig. 3. Parameters of the corrosion peak used for calculations of the quantifier, $R_{MX}$: $dm/dt$ - first derivative of mass, $m$ (mg), against time, $t$ (min); $r_X$ - height of corrosion peak (mg/min); $T_X$ - temperature of maximum corrosion peak (°C); $A$ - area of corrosion peak](image)

For the evaluation of the content of the HMC of wood specimens, a combustion method was applied (Porankiewicz 2003a,b; Porankiewicz et al. 2005, 2006). The crucibles with the ash and black particles of coal that were not burned completely were kept in a muffle oven at a temperature of 470 °C. This temperature was lower than in previous analyses so that the ash would not melt, in the case of a higher content of the potassium (K). Such a situation might result in the creation of silica particle aggregates, which had happened in a previous work (Porankiewicz et al. 2005). The combustion method was also expanded by the additional burning of the millipore glass-fiber filters at a temperature of 350 °C, as long as it was needed for black particles of charcoal to disappear. In the present study the average values of the content of the HMC from actual and previous studies were taken into account. Residues on the glass-fiber filters were examined using a scanning electron microscope (SEM). The solutions of filtrates of salt acid after digestion of ash were analyzed using energy dispersive spectroscopy (EDAX); the surface was analyzed for elemental and semiquantitative properties of calcium (Ca), potassium (K), sodium (Na), magnesium (Mg), and alumina (Al). The EDAX was also employed for analysis of hard contamination particles.

The cutting edge recession measured: $VB_S$, the clearance surface; $VB_W$, bisector of wedge angle; and $VB_F$, the rake surface (Fig. 4). The cutting edge profiles were scanned under vertical magnification of $\times50$, with the use of a stylus, perpendicular to the edge, in three paths, separated by 1 mm. The theoretical model developed is described by Eqs. 7 through 31 (Porankiewicz 2006). The predicted cutting edge recession, $VB_P$, was defined by Eq. 7. The summation of the elementary wearing effects $\Delta VB_{1ij}$ and $\Delta VB_{2ijk}$ along the cutting arc and the total feed path is given by $L_{F1,4}= 86,245$ mm for specimens nos. 1-4, whereas for specimens nos. 5 to 9 it is $L_{F5,9}= 114,993$ mm. The assumed number of fractions of the HMC was $n_f= 6$, as shown in Table 3. The cutting blade was moved for as many as $n_{cp}= 862,453$ steps for specimens nos. 1 to 4 and $n_{cp}= 1,149,938$ steps for specimens nos. 5 to 9, along the total feed paths $L_{F1,4}$ or $L_{F5,9}$. The blade was moved $n_\theta$ steps, along one single cutting arc of length 17.39 mm, from the beginning angle position $\phi_L= -0.0005$ rad to the end angle position of $\phi_U = 0.17342$ rad, inside one feed step of $f_Z= 0.1$ mm.
Fig. 4. The parameters of worn cutting edge; 0-1 - \( VB_r \) cutting edge recession measured along the rake surface; 0-2 - \( VB_W \) cutting edge recession measured along the bisector of wedge angle; 0-3 - \( VB_s \) cutting edge recession measured along the clearance surface; \( A_r \) - rake surface; \( A_c \) - clearance surface; \( P_h \) - face (main) plain; \( P_p \) - back plain; \( \gamma_F \) - contour rake angle; \( \alpha_F \) - contour clearance angle; \( \beta_F \) - contour wedge angle

\[
\Delta VB_1 = \Delta VB \cdot qdVB \cdot q_{1R} \cdot q_{1DR} \\
\Delta VB_1 = e_1 \cdot C_p f_t^2 - e_1 \cdot (C_p-D C_p f_t) ^2 \\
qdVB = e_2 \cdot e_w^e \cdot e_f^{23} \cdot ln(VB) + e_5 \\
q_{1R} = 1 + e_7 \cdot R_e^8 \text{ for } VB^p > e_6 \\
q_{1DR} = 1 + e_22 \cdot D^{23} \\
\Delta VB_{2H} = w_e S_{1H} \cdot qdVB \cdot q_{2R1} \cdot q_{2DR} \\
\Delta VB_{2J} = w_e S_{1J} \cdot qdVB \cdot q_{2R2} \cdot q_{2DR} \\
\Delta VB_{2G} = w_e S_{1G} \cdot qdVB \cdot q_{2R3} \cdot q_{2DR} \\
\Delta VB_{2F} = w_e S_{1F} \cdot qdVB \cdot q_{2R4} \cdot q_{2DR} \\
\Delta VB_{2E} = w_e S_{1E} \cdot qdVB \cdot q_{2R5} \cdot q_{2DR} \\
\Delta VB_{2D} = w_e S_{1D} \cdot qdVB \cdot q_{2R6} \cdot q_{2DR} \\
q_{2R1} = 1 + e_10 \cdot R_e^9 \text{ for } VB^p > e_6 \\
q_{2R2} = 1 + e_11 \cdot R_e^9 \text{ for } VB^p > e_6 \\
q_{2R3} = 1 + e_12 \cdot R_e^9 \text{ for } VB^p > e_6 \\
q_{2R4} = 1 + e_{13} \cdot R_e^9 \text{ for } VB^p > e_6 \\
q_{2R5} = 1 + e_{14} \cdot R_e^9 \text{ for } VB^p > e_6 \\
q_{2R6} = 1 + e_{15} \cdot R_e^9 \text{ for } VB^p > e_6 \\
q_{S_{1}} = e_{16} \cdot f_1 \\
q_{S_{2}} = e_{17} \cdot f_2 \\
q_{S_{3}} = e_{18} \cdot f_3 \\
q_{S_{4}} = e_{19} \cdot f_4 \\
q_{S_{5}} = e_{20} \cdot f_5 \\
q_{S_{6}} = e_{21} \cdot f_6 \\
q_{2DR} = 1 + e_{24} \cdot D^{25} \]

where \( VB_0 \) is the initial edge recession; \( VB^p \) is the predicted recession along the clearance
surface, along the bisector, and along the rake face which are, respectively, \( VB^F \), \( VB^W \), and \( VB^S \); \( \Delta VB_f \) is the \( VB^p \) increase due to frictional contact with wood; \( we_{2r} \cdot S_f \) is the predicted recession, \( VB^p \), effect related to the action of a single HMC particle, from its position against the edge for fraction \( f_k \); \( q_{db} \cdot S_{db} \) is the quotient for the slow down effect of \( VB^p \) with the increase of the \( VB^p \); \( q_{1R} \) is the quotient of increase of the \( VB^p \) due to HTC expressed by \( R \) quantifiers; the \( q_{1DR} \) is the quotient of increase of the cutting edge recession due to the wood density and the properties taken into account; \( \Delta VB_{2g} \) is the \( VB^p \) increase because of contact with particles of mineral contamination for fractions \( f_k \); the \( q_{2Rf} \) is the quotient of increase of the \( VB^p \) due to HTTR, expressed by the HTTR quantifiers, together with particles of HMC of fractions nos. 1 - 6; the \( q_{2DR} \) is the quotient of increase of the \( VB^p \) due to the density and the properties taken into account, together with particles of HMC, \( e_w = 2.7182818 \).

During the evaluation process, the elimination of unimportant or low important estimators by use of coefficient of relative importance (\( C_{RI} \)) defined by Eq. 3, assuming \( C_{RI} > 0.1 \), was done,

\[
C_{RI} = \left( S_K - S_{x0k} \right) \cdot S_k^{-1} \cdot 100 \% (32)
\]

where \( S_{x0k} \) is the summation of square of residuals, by estimator \( C_k = 0 \), and \( C_k \) is the estimator no. \( k \) in statistical model evaluated. The summation of residuals square, \( S_K \), standard deviation, \( S_D \), and the correlation coefficient of the predicted and observed values, \( R \), were used for characterization of approximate quality. Calculations were performed at Poznań Networking & Supercomputing Center PCSS, on a SGI Altix 3700 computer, using a special optimization program, based on a least squares method combined with gradient and Monte Carlo methods developed by the author.

**RESULTS AND DISCUSSION**

Table 3 summarizes the \( C_{MC} \), the content of ash (\( C_{AS} \)), as well as the HTTR quantifiers evaluated from TGA plots, shown in Fig. 5. Wood specimen no. 3 had the greatest hard mineral contamination, while 1, 5, 6, and 8 had low levels of contamination. The \( C_{MC} \) did not follow the \( C_{AS} \), although the \( C_{AS} \) was very high for wood specimens nos. 3 and 9, having the largest \( C_{MC} \). The \( C_{MC} \) was as high as 81.5% of the \( C_{AS} \), in case of wood specimen no. 3, while only 0.06% and 0.07% in case of specimen no. 8 and no. 5, respectively. Because of an insufficient amount of wood, evaluation of the dispersion of the HMC was not possible, but this feature of wood species originating from rain forests is large Amos (1952).

Figure 5 shows that corrosion peaks in the temperature range from 276 °C to 309 °C are very large for all of the wood specimens. They were not similar to those reported in previous works (Porankiewicz et al. 2005, 2006, 2008). The reason for that remains unknown, probably due to the operator and/or a TGA apparatus error. Low dispersion of the height of corrosion peaks, for three repetitions, can be seen for wood specimens nos. 5 and 7 (\( S_D = 0.001 - 0.004 \)), while for wood specimens nos. 1 and 3 the dispersion was much larger (0.031 - 0.034). The wood specimen no. 7 does not show the HTTR peak in the temperature range from 395 °C to 416 °C. The \( R_{As} \) quantifier was the largest of all for wood specimen no. 6, while the maximum for the other quantifiers can be seen for other species.
Table 3. Content of the HMC, $C_{MC}$(mg·kg$^{-1}$), Content of Ash, $C_{AS}$ (%), the HTTR Quantifiers $R_{As}$(mg·1$^{-1}$·mgin$^{-1}$), $R_{XS}$, $R_{WS}$, $R_{SS}$, $R_{MX}$, $R_{MI}$(min$^{-1}$)

<table>
<thead>
<tr>
<th>No.</th>
<th>$C_{MC}$</th>
<th>$C_{AS}$</th>
<th>$R_{As}$</th>
<th>$R_{XS}$</th>
<th>$R_{WS}$</th>
<th>$R_{SS}$</th>
<th>$R_{MX}$</th>
<th>$R_{MI}$</th>
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<tbody>
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<td>1</td>
<td>47.2</td>
<td>0.61</td>
<td>2.32</td>
<td>0.1013</td>
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<td>0.1198</td>
<td>0.0756</td>
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<td>275.7</td>
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<td>0.115</td>
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<td>0.0831</td>
</tr>
<tr>
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<tr>
<td>4</td>
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<td>1.783</td>
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<td>0.1194</td>
<td>0.1187</td>
<td>0.12</td>
<td>0.1007</td>
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</table>

Remarks: Average size of the $C_{MC}$ for wood specimens nos. 3, 5, 6, 7, and 9 belongs to $f_1$ (0 μm - 50 μm, average 25 μm), for specimen no. 1, there were also: 2.1 mg·kg$^{-1}$ of fraction $f_4$ (100 μm - 200 μm, average 150 μm) and 5.7 mg·kg$^{-1}$ of fraction $f_5$ (200 μm - 400 μm, average 300 μm); for specimen no. 2, there were also: 0.4 mg·kg$^{-1}$ of fraction $f_4$; for specimen no. 4, there were: 2.5 mg·kg$^{-1}$ of fraction $f_5$ and 29 mg·kg$^{-1}$ of fraction $f_6$ (400 μm - 600 μm, average 500 μm); for specimen no. 8, there were also: 30.9 mg·kg$^{-1}$ of fraction $f_2$ (50 μm - 75 μm, average 63 μm).

Fig. 5. The TGA (TG and dTG) plots of Fe with wood specimens nos. 1 - 9; $t$ - time, $T$ - temperature
Table 4. Initial Recessions of the Cutting Edge $VB_{0F}$, $VB_{0W}$, $VB_{0S}$ (mm) and their Increase $DVB_{F}$, $DVB_{W}$, $DVB_{S}$ (mm) after Total Cutting Path Length $C_{P}$ (m)

<table>
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<th>$VB_{0S}$</th>
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<td>276.9</td>
<td>71.1</td>
<td>61.1</td>
<td>20,000</td>
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</table>

Table 4 summarizes the HSS cutting edge initial recessions $VB_{0}$ and the increase of the $\Delta VB$ and the total cutting path, $C_{P}$. The largest $\Delta VB$ for specimen nos. 3 and 9 (Table 4) might be associated with very high $C_{MC}$; however specimen no. 8 had both low contamination and a very large cutting edge recession. This observation shows that exceptionally large cutting edge recession cannot be explained only by HMC, as has been done in many published papers, for example Cristóvão et al. (2009) and Cristóvão et al. (2011), while the HTTR role in the HSS tool wearing process was reported many years ago (Porankiewicz et al. 2005, 2006).

Particles of the HMC extracted from wood specimens tested in the actual study are shown in Fig. 6. In the case of all wood specimens, ball alike and irregular particles were found.

![Particles of hard mineral contamination extracted from the wood specimens nos. 1 - 9](image-url)
The size of most particles in wood specimens nos. 3, 5, 6, 7, and 9, was lower than 50 μm. In wood specimens no. 8 (also in nos. 1, 2, and 4 from a previous study (Porankiewicz et al. 2005; Porankiewicz et al. 2006; Porankiewicz et al. 2008)) several larger particles were found in the SEM images. A lack of aggregates of particles in the present combustion analysis of the HMC in all wood specimens was probably due to the lower temperature (470 °C) of additional burning of ash in a muffle oven in the present analysis. The surface of particles in the present study seems also to not be coated by a broken glaze, which was reported in earlier works (Porankiewicz et al. 2005, 2006).

![Fig. 7. Plot of EDAX analysis of HMC particles for specimens nos. 4, 5, and 6](image)

Results of the EDAX analysis of the HMC particles (Fig. 7) show that they were Si based, with a small admixture of several other elements (K, Na, Al). However, several particles in the wood specimens nos. 4 and 6 were found to be Al based, without visible impact on the ΔVB. In wood specimen no. 5, HMC particles with high or similar amount of Al and Si were found. In some particles there was evidence of small amounts of other elements (Fe, Br, F, Zn). Results of the EDAX analysis of solution of filtrates show a dominant amount of Ca in wood specimens nos. 1, 3, 4, 5, 7, and 9. The dominant amount of Mg was evidenced in wood specimens nos. 2 and 6, and dominant amount of Al was found in wood specimen no. 8.

For wood specimen no. 8, the case of low $C_{MC}$, very large cutting edge recessions were observed, $VB_{OF}$, $VB_{OW}$, and $VB_{OS}$. It is worth mentioning that for milling wood specimen no. 8 the cutting tool with the largest initial recessions was used. Low content of the $C_{MC}$ also related, to a lesser degree, to wood specimens nos. 1, 2, 4, 6, and 7, for which the cutting edge recessions were found to be much smaller. The cutting edge recessions and the $C_{MC}$ did not follow each other, although in the case of wood specimens no. 3 and 9 they did. The $D$ differs from 395 kg/m³ to 1,030 kg/m³ (Table 1), but the cutting edge recessions and the $D$ did not follow each other, especially for wood specimens nos. 3 and 9. Also wood specimen no. 7 (Kempas) had the maximum of the $CS$, the $MOR$, and the $E$ for which the cutting edge recessions was not large. This observation suggests that the role of these mechanical wood properties in the cutting edge wearing was entangled with no clear tendency. In connection with that, in the present study, the multi-parameters theoretical simulation was performed, to separate the influence of examined parameters on the increase of cutting edge recessions: the $\Delta VB_{F}$, the $\Delta VB_{W}$, and the $\Delta VB_{S}$, as well as verifying the methods of evaluation of the HTTR quantifiers ($R_{MX}$, $R_{MI}$, $R_{XL}$, $R_{WS}$, $R_{AS}$, $R_{SS}$). In the theoretical simulation, the evaluated initial cutting edge recessions ($VB_{OF}$,
$\VB_{0w}$, $\VB_{0S}$) were employed. Earlier attempts at such multi-parameters theoretical simulation were unsuccessful, probably due to unknown problems with the TGA and the use of an average value of the $\VB_0$. The best approximations for observed cutting edge recessions increase were obtained when the $R_{As}$ quantifier was employed. This suggests that the corrosion peaks for the three temperature ranges taken into account for the evaluation of the $R_{As}$ quantifier play a reasonable role in the HSS cutting edge wearing process. The plots shown in Figs. 8 through 10 were created for the HMC particles only of fraction $f_i$, minimum and average initial recessions $\VB_0$ and the cutting path length, $C_P = 10,000$ m.

The ranges of variation of the other independent variables, the $D$, the $C_{MC}$, and the $R_{As}$, were reduced in order not to exceed maximum value of observed variable, $\VB^O$. Results of theoretical simulations show (Fig. 8) that for minimum values of the initial cutting edge recession, $\VB_{0F}$, contribution of the $R_{As}$ quantifier cannot be seen, and maximum values of the $\Delta \VB_F$ for assumed maximum values of independent variables, reached 69 $\mu$m. For the average value of the initial cutting edge recession, $\VB_{0F}$, the contribution of the $R_{As}$, the $C_{MC}$, and the $D$, in an increase of the cutting edge recession measured on the clearance surface, $\Delta \VB_F$, starts from about $D = 690$ kg·m$^{-3}$ and $C_{MC} = 7800$ mg·kg$^{-1}$. Below these limits the influence of both the $D$ and the $C_{MC}$ on the $\VB_F$ is low. For the maximum value of the $\Delta \VB_F$, a synergistic effect took place of the $R_{As}$, and the mechanical wearing was as large as 54%. This means that all of these three independent variables separately have very low influence on the $\Delta \VB_F$.

For the minimum value of the $R_{As} = 1.36$, the largest $\Delta \VB_F$ decreased by half. Calculations results for the $\Delta \VB_W$ (Fig. 9), in direction of bisector of the wedge angle show much lower contributions of all independent variables in the cutting edge wearing mechanism. For the minimum values of the $\VB_{0W}$, the $\Delta \VB_W$ reached a maximum value of 37 $\mu$m, and the contribution of the $R_{As}$ in the cutting edge wearing can be seen only for larger values of the $C_{MC}$ and the $D$, when the $\Delta \VB_W$ exceeds about 10 $\mu$m, at which point the influence of the $C_{MC}$ and the $D$ also increases. For the average value of the $\VB_{0W}$, the $\Delta \VB_W$ reached a maximum value of 43 $\mu$m. In this case there was a synergistic effect of the HTTR. The mechanical wearing was as large as 13%, which was much lower than in case of the $\Delta \VB_F$.

**Fig. 8.** Plot of observed $\VB^O_F$ cutting edge recession, versus predicted one, $\VB^P_F$ obtained from theoretical simulation; black line: $R_{As} = 2.32$, red line: $R_{As} = 1.36$.
Results of calculations for the $\Delta VB_s$ (Fig. 10) show also low contribution of all independent variables in comparison to the $\Delta VB_F$. Calculations performed for minimum values of the initial cutting edge recession ($VB_{0S}$) show that maximum values of the $\Delta VB_s$ for assumed maximum values of independent variables reached $\Delta VB_s$ equal to 15.3 $\mu$m, with almost no effect of the $R_{As}$, and very small influence of the $C_{MC}$ and the $D$. For average value of the $VB_{0S} = 24$ $\mu$m, the $\Delta VB_W$ reached maximum value of 61 $\mu$m, and in this case, there was a synergistic effect of the HTTR and the mechanical wearing as large as 56%, similar to the $\Delta VB_F$.

Reduction as high as 62%, 19%, and 75% of the maximum value of respectively the $\Delta VB_F$, the $\Delta VB_W$, and the $\Delta VB_S$ was observed, when the $VB_0$ was assumed as minimum. This observation confirms a very important role of the reduction of the initial edge recessions in the resharpening process. In case of minimum of the $VB_0$ the role of
the $R_{As}$ in the HSS cutting edge wearing process was almost eliminated. Results of calculations also show that the mechanism of increase of the three analyzed recessions is different. There was a successful attempt to evaluate a theoretical model of the cutting edge recessions when milling wood originating from the rain forests of Indonesia and Japan; however, it is very complicated, so more experiments should be performed in order to get better descriptions of the examined relations. Theoretical simulations that were performed with the CS, the $MOR$, and the $E$ added to the experimental matrix did not allow to improve the quality of approximation of examined process.

CONCLUSIONS

There was a synergistic effect of the mechanical (caused by the $C_{MC}$ and the $D$) and the chemical (caused by the HTTR) factors for cutting edge recession, which increased for $\Delta V_B F$, $\Delta V_B W$, and $\Delta V_B S$, as high as 54%, 13%, and 56%, for the maximum values of the $C_{MC}$ and the $D$.

1. At the minimum values of the $V_B 0$ there was a significant reduction of the increase of the cutting edge recessions on clearance and rake surfaces.

2. The best approximation obtained for the $R_{As}$ quantifier suggest that corrosion peaks for the three temperature ranges taken into account play a reasonable role in the HSS cutting edge wearing process.

3. The separate influence of analyzed independent variables (the $R_{As}$, the $C_{MC}$, and the $D_F$) at minimum values of the others was low.

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**APPENDIX**

The following estimators for Eqs. 7 to 31, for the $\Delta VB_F$, were evaluated: $e_1= 105.80111$; $e_2= 0.1914$; $e_3= 0.87242$; $e_4= 1.81659$; $e_5= -5.98367 \cdot 10^{-2}$; $e_6= 47.29786$; $e_7= 0.5611$; $e_8= 8.10204$; $e_9= 3.27943$; $e_{10}= 17.64729$; $e_{11}= 0.39162$; $e_{12}= 9.94742 \cdot 10^{-6}$; $e_{13}= 1.05509 \cdot 10^{-6}$; $e_{14}= 1.23453 \cdot 10^{-7}$; $e_{15}= 6.977 \cdot 10^{-9}$; $e_{16}= 7.86738 \cdot 10^{-2}$; $e_{17}= 6.84019 \cdot 10^{-2}$; $e_{18}= 9.5875 \cdot 10^{-6}$; $e_{19}= 9.98129 \cdot 10^{-7}$; $e_{20}= 1.30198 \cdot 10^{-7}$; $e_{21}= 8.179 \cdot 10^{-9}$; $e_{22}= 0.838$; $e_{23}= 0.32098$; $e_{24}= 0.27857$; and $e_{25}= 8.1909 \cdot 10^{-2}$, by summation of square of residuals as high as $S_K=729.5$, correlation coefficient between predicted the observed recessions as high as $R=0.998$ and the standard deviation $S_D=9.1$.

The following estimators for Eqs. 7 to 31, for the $\Delta VB_W$, were evaluated: $e_1= 12.4821$; $e_2= 0.18063$; $e_3= 0.58194$; $e_4= 1.67074$; $e_5= -3.69965 \cdot 10^{-2}$; $e_6= 19.8861$; $e_7= 0.22358$; $e_8= 5.90069$; $e_9= 0.15666$; $e_{10}= 10.64828$; $e_{11}= 2.09201$; $e_{12}= 1.1 \cdot 10^{-5}$; $e_{13}= 9.5323 \cdot 10^{-7}$; $e_{14}= 1.07756 \cdot 10^{-7}$; $e_{15}= 1.1 \cdot 10^{-8}$; $e_{16}= 1.59231 \cdot 10^{-2}$; $e_{17}= 36.34688$; $e_{18}= 1.1 \cdot 10^{-5}$; $e_{19}= 1.1 \cdot 10^{-6}$; $e_{20}= 1.1 \cdot 10^{-7}$; $e_{21}= 1.1 \cdot 10^{-8}$; $e_{22}= 0.75586$; $e_{23}= 0.29782$; $e_{24}= 0.15707$; and $e_{25}= 7.38522 \cdot 10^{-2}$; by: the $S_K=338.6$, the $R=0.989$ and $S_D=6.4$.

The following estimators for Eqs. 7 to 31, for the $\Delta VB_S$, were evaluated: $e_1= 11.91796$; $e_2= 0.34643$; $e_3= 0.34349$; $e_4= 1.59324$; $e_5= -2.2916 \cdot 10^{-2}$; $e_6= 24.88184$; $e_7= 0.32224$; $e_8= 3.31983$; $e_9= 2.94091$; $e_{10}= 5.14568$; $e_{11}= 1.21621$; $e_{12}= 10^{-5}$; $e_{13}= 7.52823 \cdot 10^{-7}$; $e_{14}= 9.4074 \cdot 10^{-8}$; $e_{15}= 1.0217 \cdot 10^{-8}$; $e_{16}= 1.16367 \cdot 10^{-2}$; $e_{17}= 23.35736$; $e_{18}= 9.32246 \cdot 10^{-6}$; $e_{19}= 7.05635 \cdot 10^{-7}$; $e_{20}= 1.25084 \cdot 10^{-7}$; $e_{21}= 8.34710^{-9}$; $e_{22}= 1.14348$; $e_{23}= 0.28774$; $e_{24}= 6.83483 \cdot 10^{-2}$; and $e_{25}= 5.53764 \cdot 10^{-2}$; by: $S_K=204.2$, the $R=0.989$ and the $S_D=5.1$. 